

# Ma 221. Syllabus. Summer 2013.

Instructors:

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Classes: MTWR 2:00-4:00, Morton 103.

Office hours:

P.Dubovski: Kidde 226, M, W 1-2 and by appointment.

Textbook:

[1] Nagle, Saff, and Snider, "Fundamentals of Differential Equations and Boundary Value Problems," 6<sup>th</sup> edition, Addison Wesley. ISBN 032161321X

[2] M.Tenenbaum and H.Pollard, "Ordinary Differential Equations", Dover. ISBN 0486649407.

## Syllabus:

### Week 1 (May 16-17)

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| 1.1-1.3 Direction Fields. Isoclines  | 1.1: # 1-17.<br>1.2: # 1, 2, 9, 10, 20, 21, 23-28, 30, 31.<br>1.3: #3, 4, 5, 7, 9, 17, 18.  |
| 1.4, 1A, 1D. Euler method.<br>Taylor series method.<br>Phase portrait: Fixed points, Stability | 1.4 # 6, 10, 15, 16.<br>1A. Using Taylor series method, solve the following equations. Estimate the convergence interval for the series:<br>(1) $y'+3y=x^2$ , $y(0)=1$ .<br>(2) $y''-y=1$ , $y(0)=1$ .<br>1D. Sketch phase portrait for equations:<br>(1) $y'=y(1+y)(2-y)$<br>(2) $y'=y(1+y)(2-y)^2$<br>(3) $y'=y(1+y)(2-y)^3$<br>(4) $y'=y^2-5y+6$<br>Find fixed points and determine, which of them are stable, unstable, or neither. |
| <b>Hw1</b> due on Wednesday 5/22   | 1.2: # 2, 10, 20<br>1.3: # 5<br>1.4: # 6<br>Using Taylor series method, solve equation $y'+3y=x^2$ , $y(0)=1$ .<br>Sketch phase portrait for equation $y'=y(1+y)(2-y)$ .  |

**Week 2 (May 20-24)**

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| 2.1, 2.2, 2.3 Separable equations. Linear Equations: Integrating factor, Variation of parameters. | 2.2: #7,8,13,15,16,18,20,26,27(a-c),34,38<br>2.3: #7,8,14,15,18,20,21,22,30,32,33.   |
| 2.4 Exact Equations   | 2.4: # 10, 11, 13, 14, 19, 22, 23, 25, 27, 28, 29, 30, 31, 33(a-d).  |
| 2.5, 2.6 Integrating factors. Substitutions.  | 2.5: # 7, 9, 10, 11, 13, 14, 15, 17, 18<br>2.6: # 11, 12, 13, 15, 18, 19, 20, 41.  |
| 2.6, 2D Transformations   | 2.6: # 21, 22, 23, 24, 25, 26, 27, 28, 31, 32, 42  |
| Chapter 2 – review;<br>2E – Clairaut equation   | Review # 1-15, 31-35;<br>2.6 # 33-40, 43;<br>2E # (d,e).   |
| Ch. 2 –review; 2H – asymptotics;<br>Integral curves; Riccati eqn.                                 | Review # 16-30, 36-40; # 3 (p.82);<br>2E (a-e);<br>2.6: #45, 46  |
| <b>Hw2</b> due on Tuesday 5/28  | 2.2: # 8, 16, 18, 38<br>2.3: # 8, 14, 18, 20, 22, 30<br>2.4: # 10, 14, 22, 28, 30<br>2.5 # 10, 14<br>2.6 # 24, 26, 28, 34, 36, 38<br>Review # 4, 8, 12, 16, 20, 24, 28, 32, 36, 40<br>2E (d) |

**Week 3 (May 28-31)**

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| 4.1, 4.2, 4.3<br>Homogeneous second-order linear equations<br><br>4.4, 4.5, 4.6 Inhomogeneous linear equations | 4.1: # 4, 5, 7, 8<br>4.2: # 1, 2, 3, 4, 13, 14, 15, 16, 17, 18<br>4.3: # 9-14, 21-26, 28, 31, 32, 34<br>4.4: # 9-14<br>4.5 # 17-22, 23-30<br>4.6: # 1-10   |
| 6.1, 6.2<br><br>Eigenvalue problems  | 6.1: # 16, 17, 19, 20<br>6.2: # 1-6, 15, 19-21<br>Solve equations:<br>(1) $y''+y'-2y=0$ , $y(0)=0$ , $y(1)=1$<br>(2) $2y''+y'-3y=1$ , $y(0)=1$ , $y(1)=0$<br>(3) $y''+y'-2y=x$ , $y(0)=2$ , $y(1)=1$<br>Find $\lambda$ for which the following equations have nonzero solutions:<br>(4) $y''+\lambda y=0$ , $y(0)=y(1)=0$ .<br>(5) $y''+\lambda y=0$ , $y(0)=y(\pi)=0$ .<br>(6) $y''+\lambda y=0$ , $y(0)=y(L)=0$ .<br>(7) $y''+\lambda y=0$ , $y'(0)=y(L)=0$ .<br>(8) $y''+\lambda y=0$ , $y(0)=y'(L)=0$ .<br>(9) $y''+\lambda y=0$ , $y'(0)=y'(L)=0$ . |
| <b>Hw3</b> due on Wednesday 6/5  | 4.1: # 8<br>4.2: # 2, 14<br>4.3: #10, 28, 32<br>4.4: # 10, 14<br>4.5: # 18, 22, 30<br>4.6: # 2, 6<br>6.1: # 16, 20<br>6.2: # 4, 6, 20  |

**Week 4 (June 3-7)**

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| 4.7 Cauchy-Euler equations.<br>Reduction of Order<br>7.2, 7.3, 7.4, 7.5, 7.6, 7.7, 7.8 | 4.7 # 9-18, 19-20, 37-40, 41-43, 44, 45-49<br><br>7.8 # 14-20;<br>7.7 # 15-22<br>7.6 # 29-37 |
| <b>No Hw due this week</b>   |  |

**Week 5 (June 10-14)**

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| PDEs<br>10.2, 10.3, 10.4, 10.5, 10.6, 10.7 | 10.2 # 9-14, 15-18<br>10.5 # 1-5, 9, 10, 13, 14.<br>10.6 # 1-4, 7, 8, 13-18<br>10.7 # 1-5, 7, 8, 11-13.   |
| <b>Hw4 due on Tuesday 6/18</b>             | 4.7 # 10<br>7.8 # 20<br>7.7 # 22<br>7.6 # 36<br>10.2 #14<br>10.5 # 4, 14<br>10.6 # 4, 8.<br>10.7 # 4, 12. |

**Week 6 (June 17-21)**

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| MT – Review<br>Wednesday 6/19 – midterm exam<br>Thursday – solution of the exam. | <b>Review all the above problems</b> |
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**Final Exam (cumulative): Saturday June 29.**